

Physical Interpretation of Maxwell's
Eqⁿ or Integral form
of Maxwell's Eqⁿ :-

Maxwell's I eqⁿ :-

From the Maxwell's I eqⁿ,
we know that

$$\text{Div } \mathbf{D} = \rho$$

Now, taking the volume integral
of above eqⁿ, we get

$$\int \text{Div } \mathbf{D} \, dv = \int \rho \, dv \quad \text{--- (1)}$$

we have

$$q = \int \rho \, dv$$

then above eqⁿ converts in the
form of

$$\int \text{Div } \mathbf{D} \, dv = q$$

Applying the Gauss Divergence theorem

in above eqⁿ, we get

$$\int \mathbf{D} \cdot d\mathbf{s} = q$$

This is the integral form of Maxwell I eqⁿ which can be expressed as the surface integral of electric displacement vector is equal to the total charge flowing in the surface.

Maxwell II eqⁿ :-

From Maxwell's II eqⁿ :-

$$\text{Div } \mathbf{B} = 0$$

on taking the volume integral, we get

$$\int \text{Div } \mathbf{B} \, dV = 0$$

Now using the Gauss Divergence theorem in above eqⁿ, we get

$$\int \mathbf{B} \cdot d\mathbf{s} = 0$$

This is the Maxwell's II eqⁿ

which can be interpreted as the surface integral of magnetic field is continuous, i.e., the magnetic monopoles does not exist and magnetic lines of force form close loop.

3. Maxwell's III eqⁿ :-

From Maxwell III eqⁿ the curl of magnetic field intensity is equal to the sum of conduction current and displacement current density.

$$\text{Curl } H = J + J_d$$

Now taking the surface integral of above eqⁿ, we get

$$\int \text{Curl } H \cdot ds = \int J \cdot ds + \int J_d \cdot ds$$

Also from the definition of current density, we know that

$$I = \int J \cdot ds$$

similarly, $I_d = \int J_d \cdot ds$

$$\oint \text{curl } H \cdot ds = I + I_d$$

Now, using the Stoke's theorem of above eqⁿ we get

$$\boxed{\int H \cdot dl = I + I_d}$$

$B = \mu_0 H$
 $\Rightarrow B = \mu_0 (I + I_d)$

This is the integral form of Maxwell III eqⁿ which shows that the line integral of magnetic field intensity is equal to the sum of conduction current and displacement current.

4. Maxwell IV eqⁿ :-

From Maxwell IV eqⁿ we know that

$$\text{curl } E = - \frac{\partial B}{\partial t}$$

Now taking the surface integral of above eqⁿ, we get

$$\int \text{curl } E \cdot ds = - \int \frac{\partial B}{\partial t} \cdot ds$$



$$\int \text{curl } E \, ds = -\frac{d}{dt} \int B \cdot ds$$

We also know that

$$d\phi = B \cdot ds$$

$$\phi = \int B \cdot ds$$

then from above eqⁿ, we get

$$\int \text{curl } E \, ds = -\frac{d\phi}{dt}$$

by using the Stoke's theorem the surface integral can be converted into line integral.

$$\int E \cdot dl = -\frac{d\phi}{dt}$$

This is the integral form of Maxwell IV eqⁿ which shows that the line integral of electric field intensity is equal to the negative rate of change of magnetic flux.